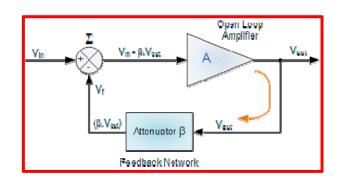


Feedback analysis

Originates in early amplifier design & control systems theory



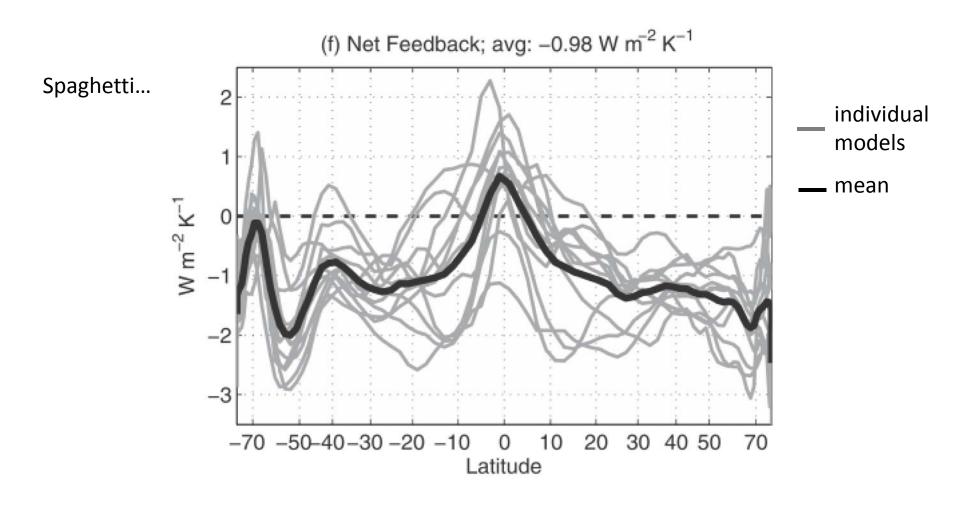
- Formal method for evaluating how interacting components of a dynamical system combine to give the system response.
- For climate at the global scale, there is well-oiled machinery

$$\Delta T = \lambda_0 \frac{\Delta R_f}{1 - \sum_i f_i}$$
 $\Delta T = \text{response}$ $\Delta R_f = \text{forcing}$ $f_i = \text{feedback factors}$

- How does uncertainty in physical process lead to uncertainty in climate response?
- What happens when it is applied to the regional scale?

The spread in zonal mean feedbacks in CMIP3 models

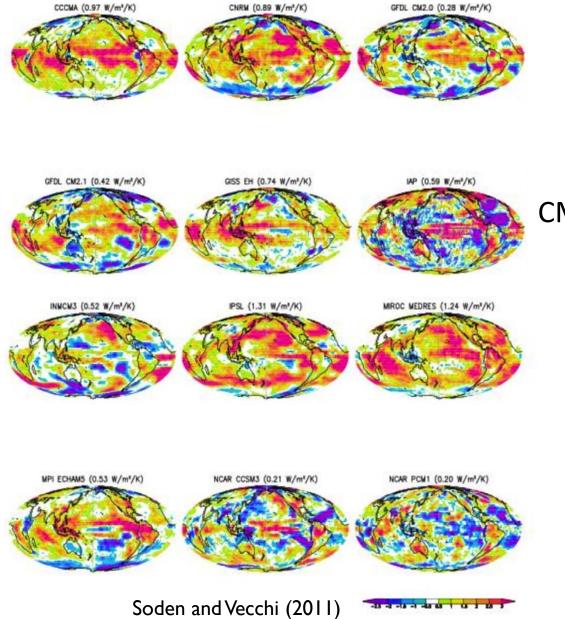
(Zelinka and Hartman, 2011)



• If it were possible to discriminate among the strands, what would be consequences for the local and nonlocal climate response?

The variation in cloud feedbacks in CMIP3 models

Soden and Vecchi, 2011



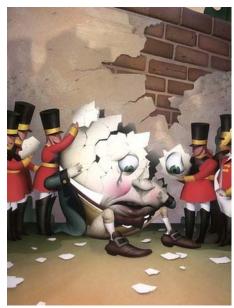
Net cloud feedback among CMIP3 models

Regional feedbacks

Some questions

 Are the regional feedbacks <u>linear enough</u> to have predictive power?

(i.e., can you put the pieces back together again?)



The Humpty Dumpty challenge

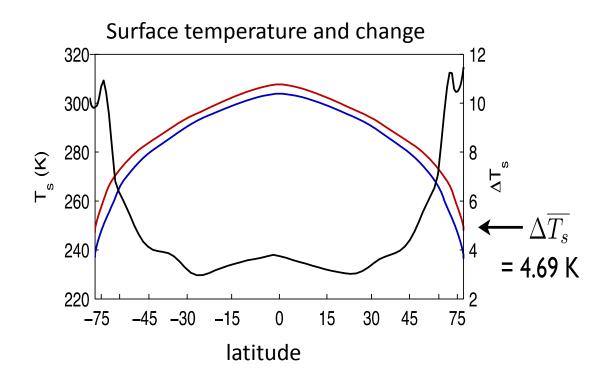
 How does uncertainty in the physics of one region affect uncertainty in the response of another region?

(i.e., how do tropical clouds feedbacks affect polar amplification?)

A stripped down climate model (Nicole Feldl's PhD)

GFDL AM2 model

- Aquaplanet, perpetual equinox, 20-m mixed layer, simple sea ice,
- 2×CO₂ to equilibrium



Climate sensitivity of 4.69K

Deconstructing the local energy balance

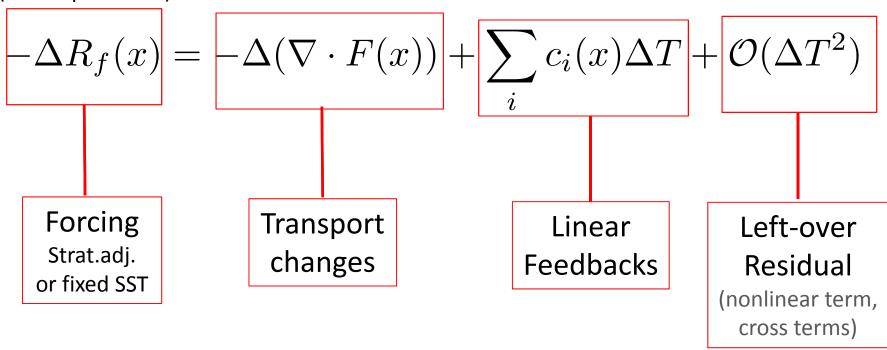
A Taylor series of the local TOA energy balance: (new equilibrium)

$$-\Delta R_f(x) = -\Delta(\nabla \cdot F(x)) + \sum_i c_i(x)\Delta T + \mathcal{O}(\Delta T^2)$$

Deconstructing the local energy balance

A Taylor series of the local TOA energy balance:

(new equilibrium)



How to get the coefficients, the c_i 's?

Deconstructing the local energy balance

A Taylor series of the local TOA energy balance:

$$-\Delta R_f(x) = -\Delta(\nabla \cdot F(x)) + \sum_i c_i(x)\Delta T + \mathcal{O}(\Delta T^2)$$

The Kernel method for feedbacks (Soden and Held, 2006)

Build the partial derivatives:

$$c_i = \frac{\partial R}{\partial \alpha} \frac{\Delta \alpha}{\Delta T}$$

 α is temperature, water vapor, clouds, surface albedo

Deconstructing the local energy balance

A Taylor series of the local TOA energy balance:

$$-\Delta R_f(x) = -\Delta(\nabla \cdot F(x)) + \sum_i c_i(x)\Delta T + \mathcal{O}(\Delta T^2)$$

The Kernel method for feedbacks (Soden and Held, 2006)

Build the partial derivatives:

$$c_i = \frac{\partial R}{\partial \alpha} \frac{\Delta \alpha}{\Delta T}$$

 α is temperature, water vapor, clouds, surface albedo

The Kernel, K_i : built from one year of six-hourly calls to the stand-alone radiation code, nudging each variable by a small amount $\frac{\text{keeping everything else constant}}{\text{and then doing a lot of averaging.}}$ (Nicole built custom kernels for this set-up)

Deconstructing the local energy balance

A Taylor series of the local TOA energy balance:

$$-\Delta R_f(x) = -\Delta(\nabla \cdot F(x)) + \sum_i c_i(x)\Delta T + \mathcal{O}(\Delta T^2)$$

The Kernel method for feedbacks (Soden and Held, 2006)

Clouds are too messy, so

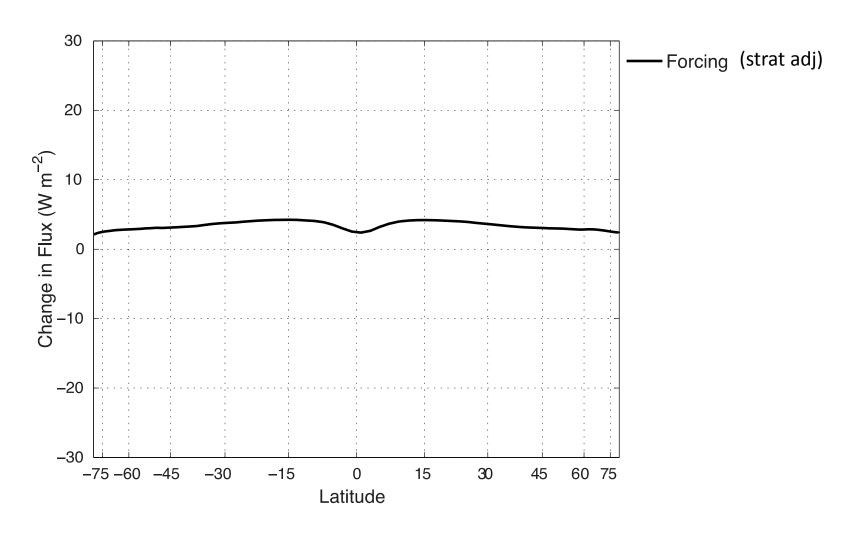
$$c_{cld}\Delta T = \Delta {
m CRF} + \sum_i (K^o_{lpha_i} - K_{lpha_i}) dlpha$$
 ud radiative forcing

 Δ CRF = cloud radiative forcing

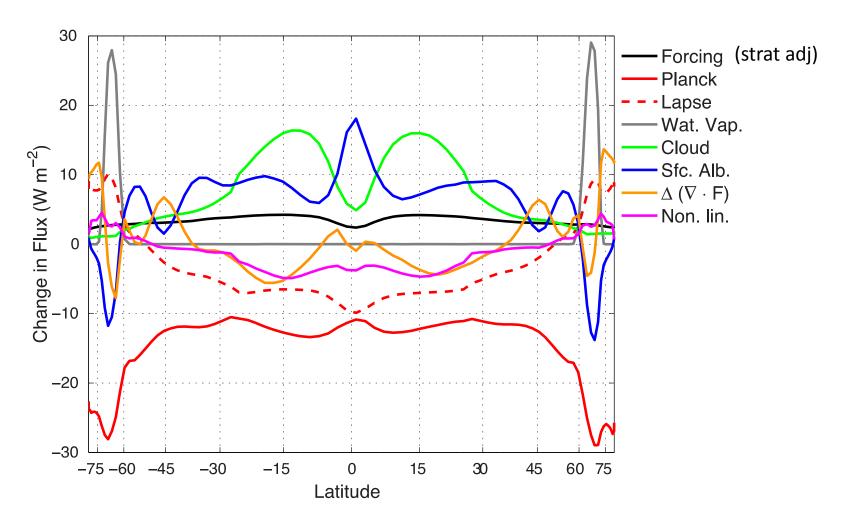
Corrections to account for overlap

 There are other ways of calculating feedbacks, but Kernels comes closest to the tangent linear calculation underlying the feedback concept.

First, he pieces of the local energy budget in W m⁻²



First, the pieces of the local energy budget in W m⁻²



- The forcing is a small term in the budget compared to the responses.
- Climate prediction is hard!

An aside: the definition matters...

Taylor series:

$$-\Delta R_f(x) = -\Delta(\nabla \cdot F(x)) + \sum_i c_i(x)\Delta T + \mathcal{O}(\Delta T^2)$$

Can have either globally or locally defined feedbacks:

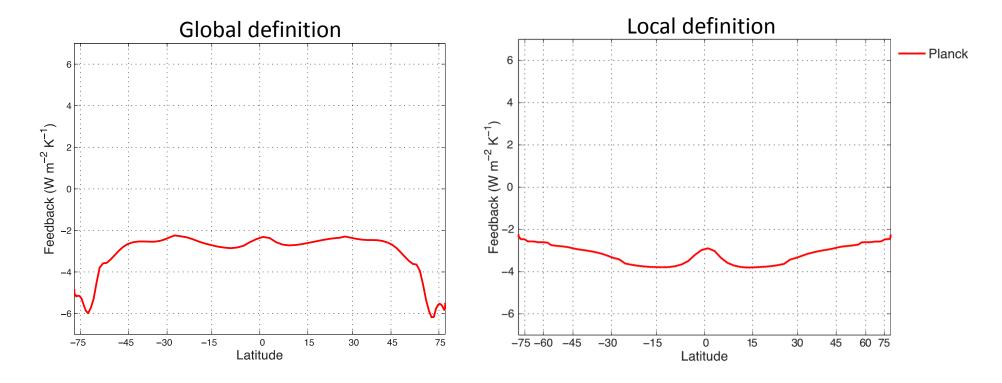
$$c_i = rac{\partial R}{\partial lpha} rac{\Delta lpha}{\overline{\Delta T}}$$
 Can use $\Delta T(x)$ or $\Delta T>$

An aside: the definition matters...

Taylor series:

$$-\Delta R_f(x) = -\Delta(\nabla \cdot F(x)) + \sum_i c_i(x)\Delta T + \mathcal{O}(\Delta T^2)$$

Example: Planck "Feedback" (i.e., you think of this as $4\sigma T^3$)

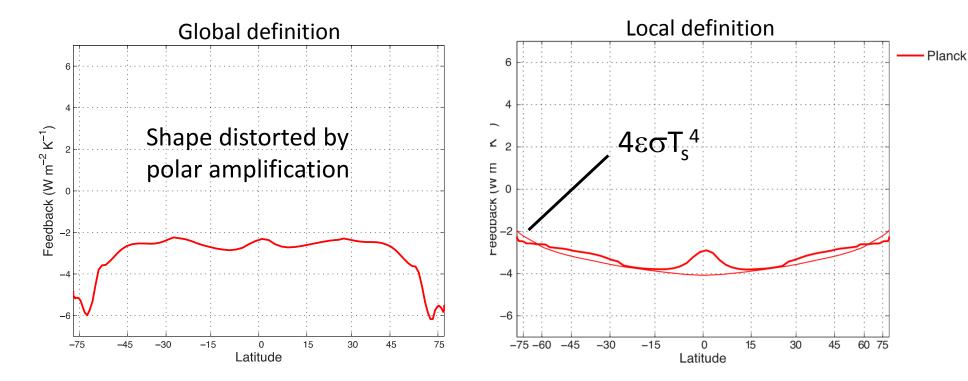


An aside: the definition matters...

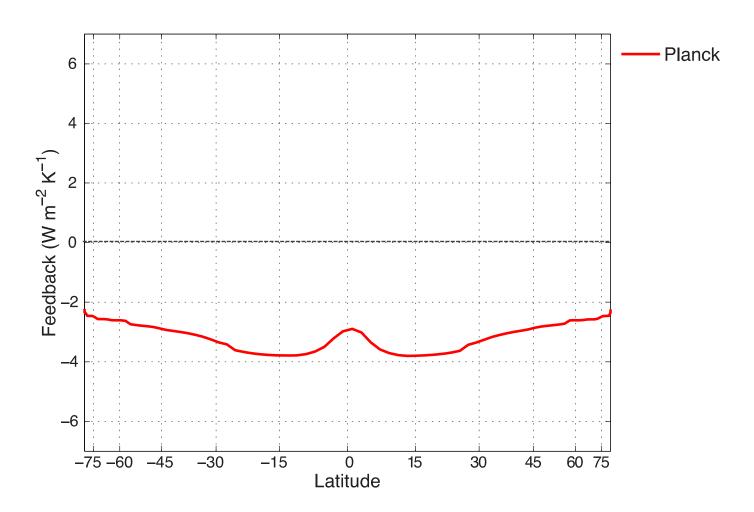
Taylor series:

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Example: Planck "Feedback" (i.e., you think of this as $4\sigma T^3$)

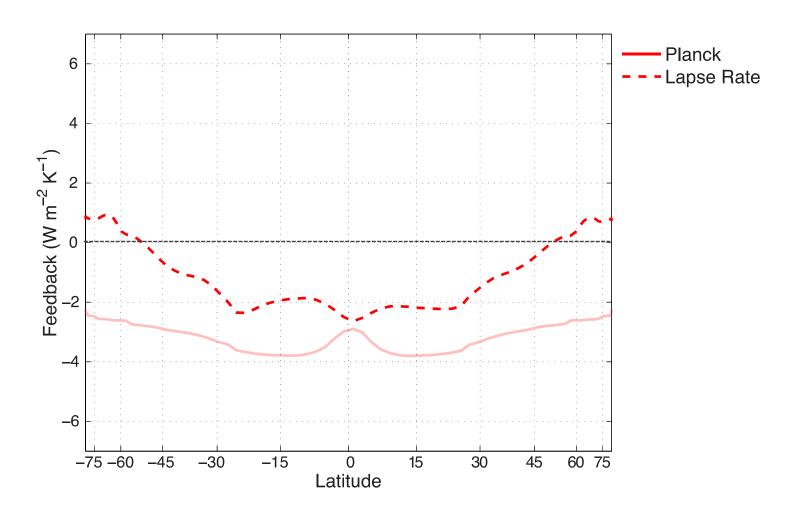


(locally defined)



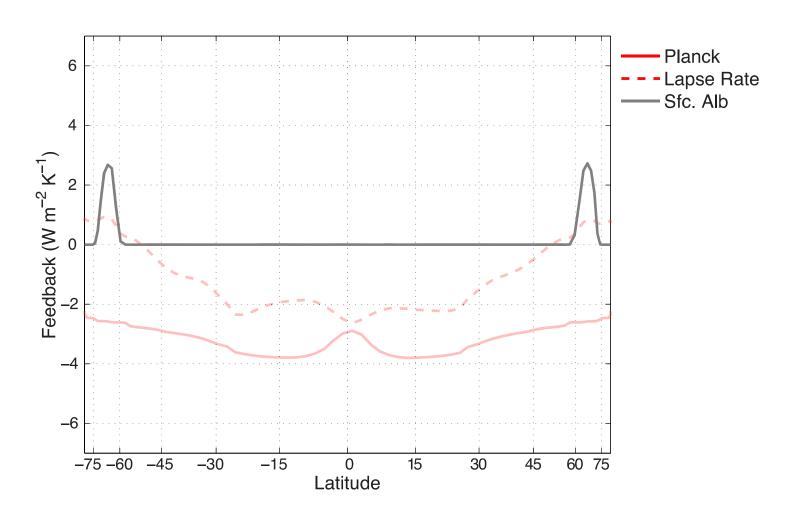
• Deep clouds mask temperature response in deep tropics...

(locally defined)



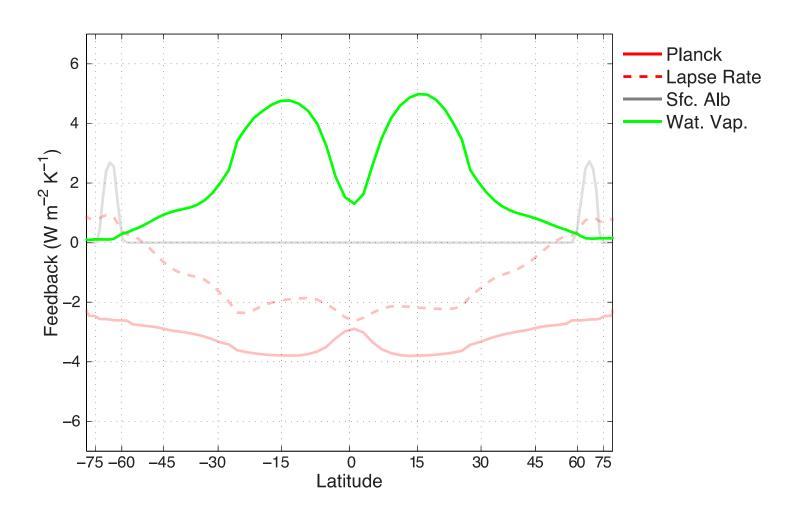
Lapse rate is negative (strongest in tropics)
 (+ve at high latitudes where there are T inversions)

(locally defined)



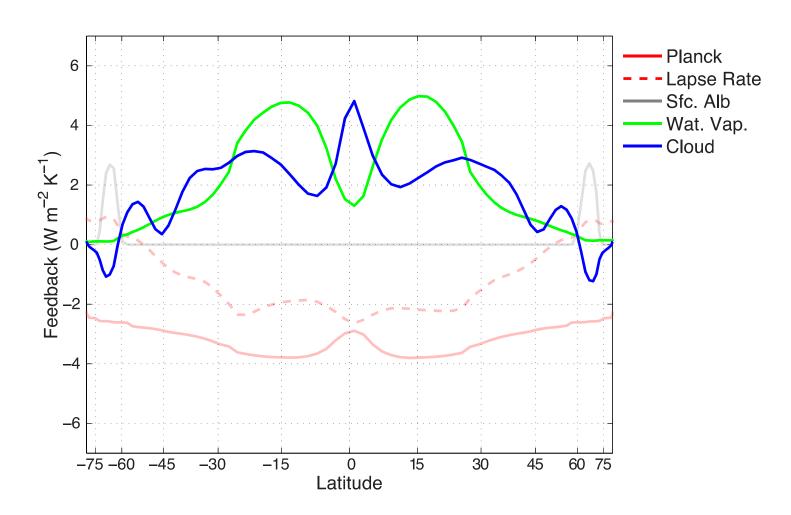
• Ice albedo feedback only operates at the ice line.

(locally defined)



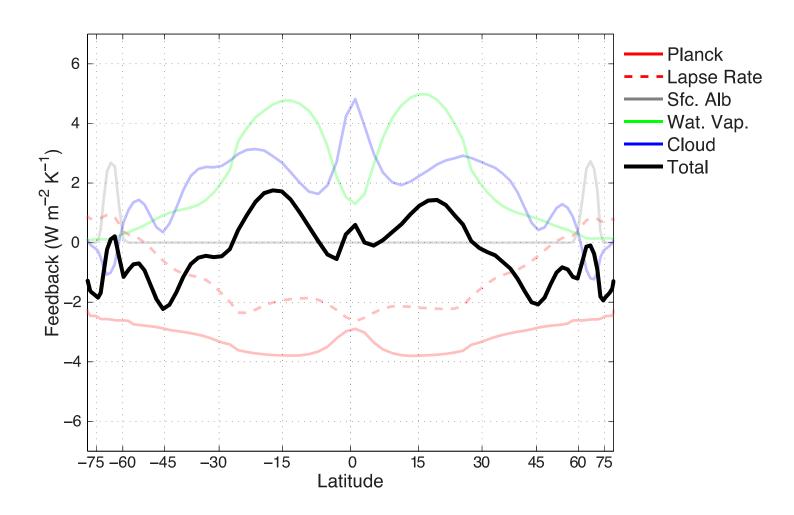
Water vapor feedback is strongest in subtropics (clear skies).

(locally defined)



- Cloud feedback generally +ve (due to decrease in cloud fraction).
- Can see covariance among feedback patters (tropics and ice line)

(locally defined)

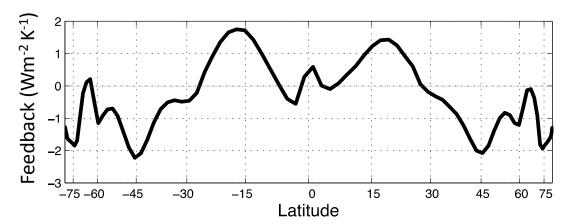


- Locally unstable ($\Sigma_i c_i > 0$) in the tropics and ice line.
- Strongest +ve feedbacks in tropics, where response is weakest (weird)

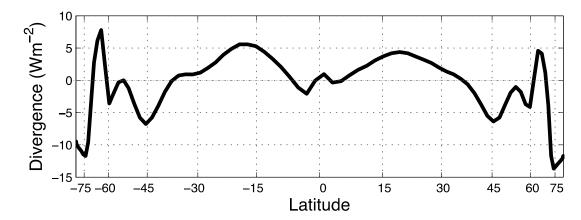
Key result: Feedback patterns drive transport changes

Net linear feedback

$$c_{tot}(x) = \sum_{i} c_i(x)$$



Transport changes from model $\Delta(\nabla \cdot F)$

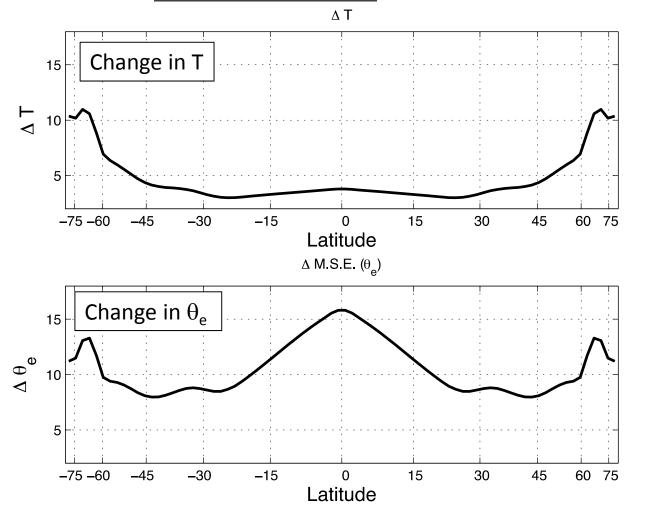


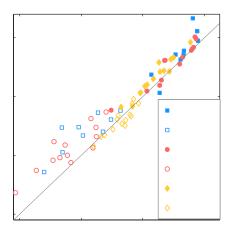
Three implications:

- Kernel method works (phew!)
- System exports energy away from regions of +ve feedbacks and towards regions of negative feedbacks
- Transport/circulation changes are slave to the feedbacks(!)

Ting and Dargan's Big Idea:

 Hwang and Frierson (2010) showed that, after subtracting the s.w. & cld impacts, inter-model differences in transport changes were consistent with diffusion of moist static energy.

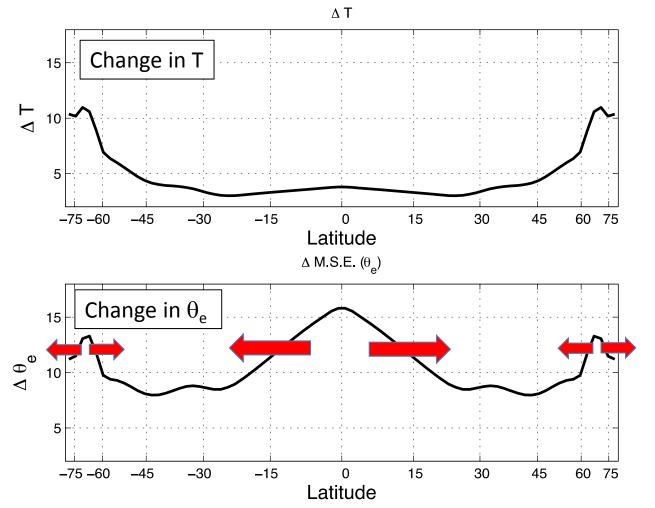


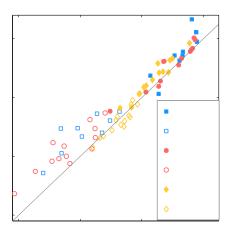


Hwang and Frierson (GRL, 2010)

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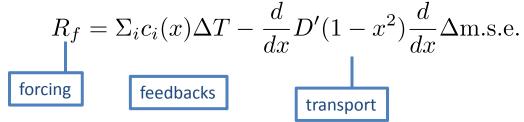


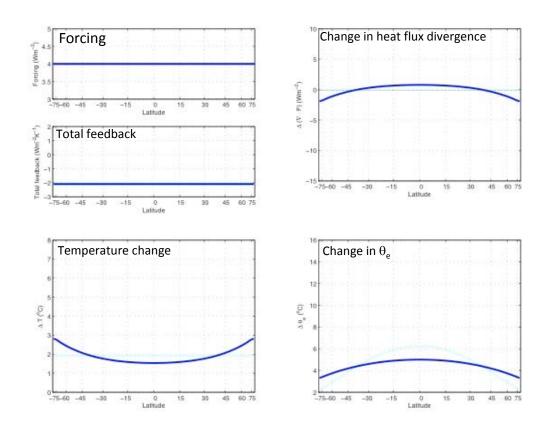
Hwang and Frierson (GRL, 2010)

How well does a moist EBM do?

Diffuse moist static energy:

Uniform feedbacks





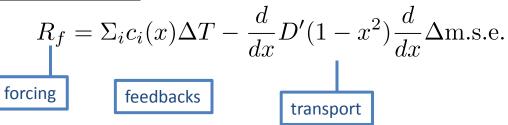
Result:

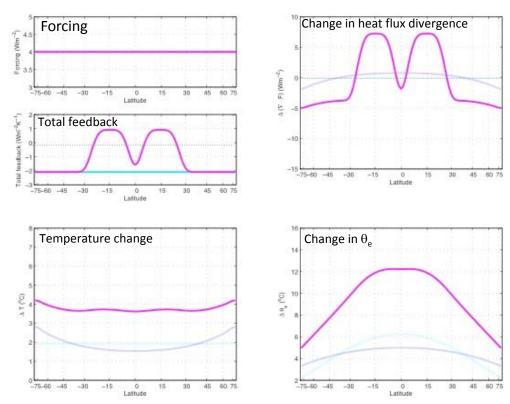
Divergence of m.s.e from tropics convergence at high latitudes Some polar amplification from this alone,

How well does a moist EBM do?

Diffuse moist static energy:

Add strong, locally unstable tropical feedbacks





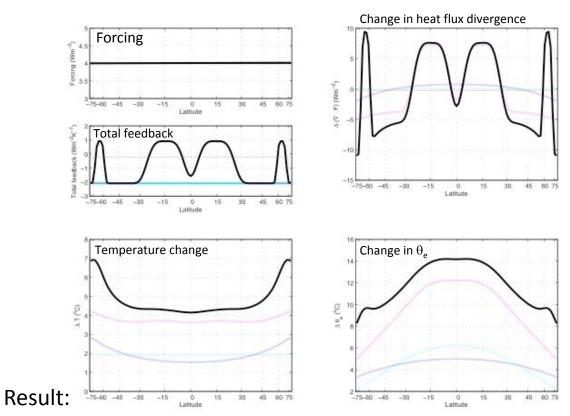
Result:

Larger divergence of m.s.e from +ve feedback regions Polar amplification remains, despite stronger feedbacks in tropics! Anomalous transport is up the T gradient, but down the θ_e gradient

How well does a moist EBM do?

Diffuse moist static energy:
Add strong locally unstable
feedbacks at the ice lines too

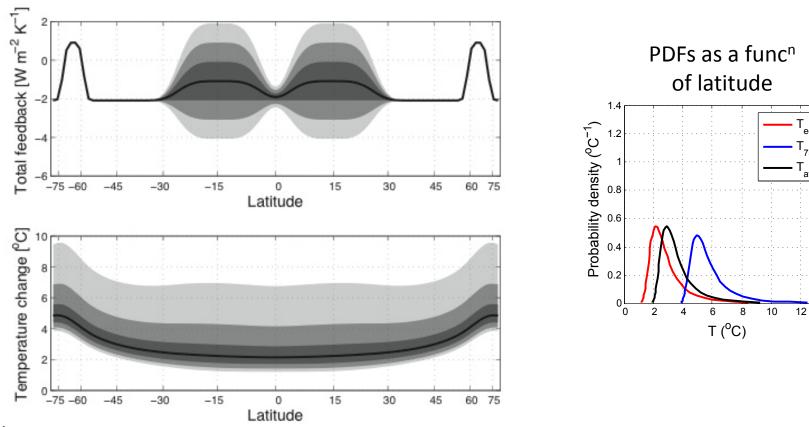
$$R_f = \Sigma_i c_i(x) \Delta T - \frac{d}{dx} D' (1-x^2) \frac{d}{dx} \Delta \text{m.s.e.}$$
 forcing feedbacks transport



- -Large divergence of m.s.e. from +ve feedback regions (incl. away from the ice line)
- -Polar amplifications strongly enhanced; convergence of energy polewards of ice line
- -Climate sensitivity is increasing rapidly as global mean feedback approaches zero These all look a lot like the diagnosed behavior of Nicole's aquaplanet...

How does uncertainty in local feedbacks translate to uncertainty in the local and nonlocal climate response?

Vary strength of tropical feedbacks, consider pattern of climate response: Top panel: hypothetical 1σ , 2σ , 3σ ranges in tropical feedback (made up, obviously) Bottom panel: the climate response as a function of latitude.

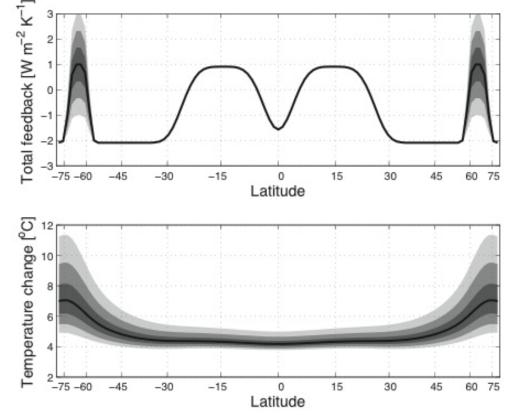


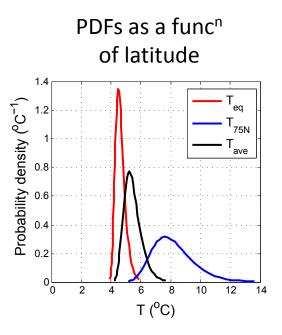
Results:

Overall skewed envelope of temperature response (just like the global case) Uncertainty in response is spread to all latitudes

How does uncertainty in local feedbacks translate to uncertainty in the local and nonlocal climate response?

Vary strength of polar feedbacks, consider pattern of climate response: Top panel: hypothetical 1σ , 2σ , 3σ ranges in sfc albedo feedback (made up, obviously) Bottom panel: the climate response as a function of latitude.





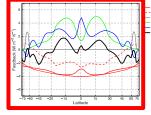
Results:

Overall skewed envelope of temperature response (just like the global case) Uncertainty is largely confined to the high latitudes

Summary

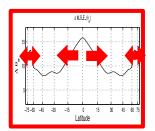
- Kernel-based feedbacks combine to provide physicallymeaningful patterns.
- The feedback patterns are dictated by the climatological circulation, but the climate response is dictated by the pattern of feedbacks



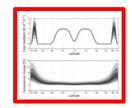


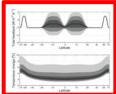


- Energy is driven away from regions of strong positive feedbacks towards regions of more negative feedbacks (& two scales to polar amplification).
- Simple down gradient transport of m.s.e. anomalies explains much of the model behavior



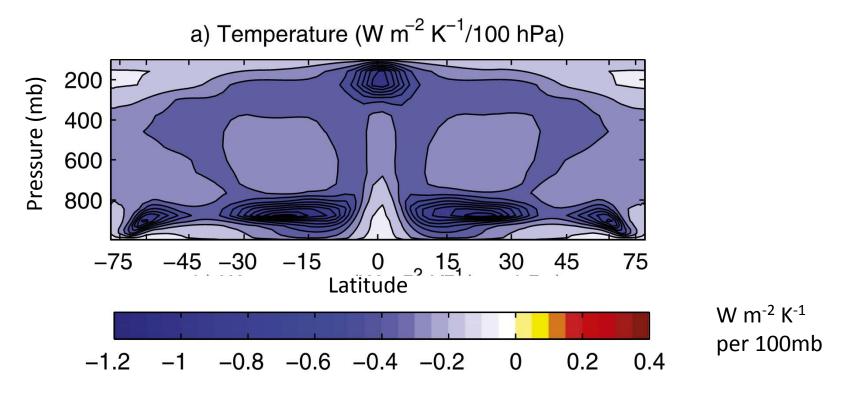
 Uncertainty in tropical process have a global impact/ uncertainty in polar processes confined largely to poles





Some examples of Kernels

The temperature kernel, $\partial R/\partial T$

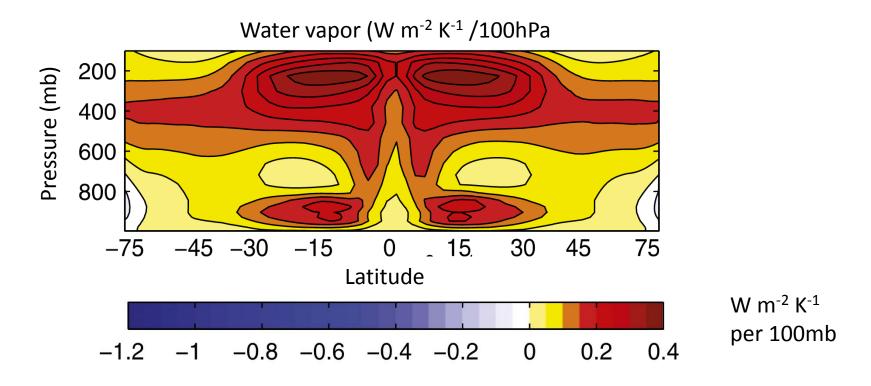


- Negative everywhere
- Biggest impact is from temp changes above cloud tops
- Temperature changes are *masked* beneath clouds

Some examples of Kernels

The water vapor kernel, $\partial R/\partial q$

(albeit in weird units)



- Positive everywhere (except at low levels and very high latitudes)
- TOA acutely sensitive to upper tropospheric humidity changes, (especially above cloud tops)

Partial temperature decomposition

Back to Taylor series

$$-\Delta R_f(x) = -\Delta(\nabla \cdot F(x)) + \sum_i c_i(x)\Delta T + \mathcal{O}(\Delta T^2)$$

Rearrange:

 $c_{PI}(x) = Planck$ "feedback"

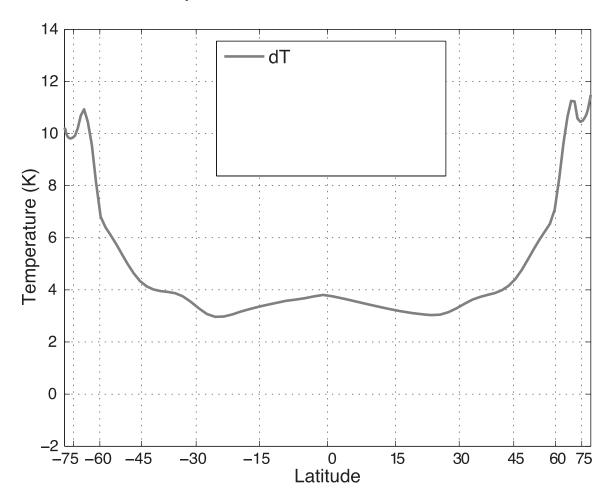
$$\Delta T_s(x) = \frac{1}{c_{Pl}(x)} \left[\Delta(\nabla \cdot F(x)) - \Delta R_f(x) - \mathcal{O}(\Delta T^2) - \left(\sum_{i \neq P} c_i\right) \Delta T_s(x) \right]$$

Decompose the local temperature change into its constituent causes:

Relates to original (i.e., proper) feedback factors:

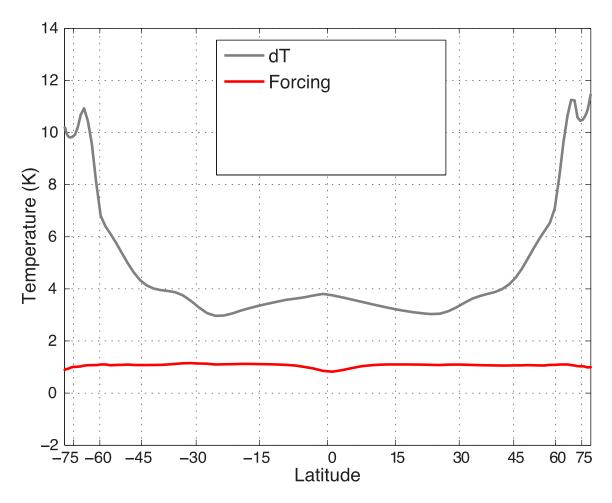
$$\Delta T_s(x) = \lambda_0 \frac{\Delta R_f - \Delta(\nabla \cdot F)}{1 - \sum_i f_i(x)} \quad \text{where } f_i(x) = -\frac{c_i(x)}{c_{Pl}(x)}$$

Partial temperature decomposition



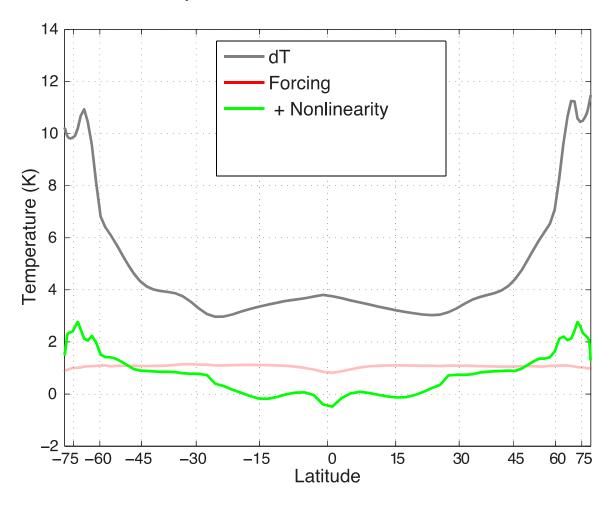
How do the pieces add up to this response?

Partial temperature decomposition



Forcing provides nearly uniform ~1.0°C

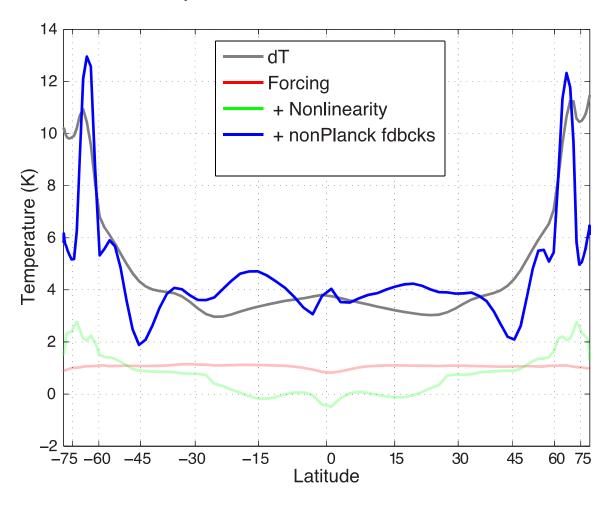
Partial temperature decomposition



Nonlinearity also fairly small ~+/-1.0°C

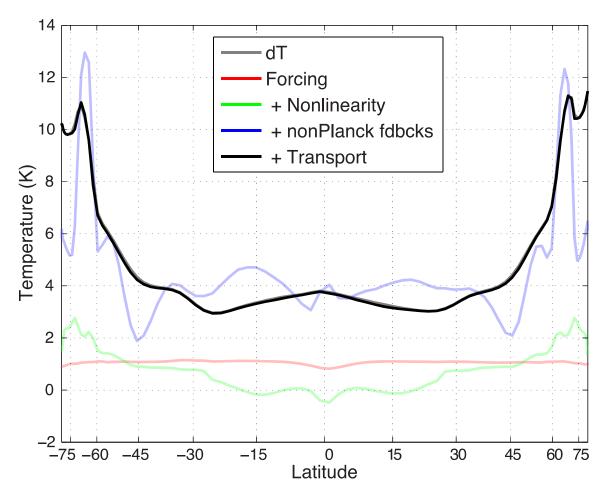
(& due to clear-sky masking)

Partial temperature decomposition



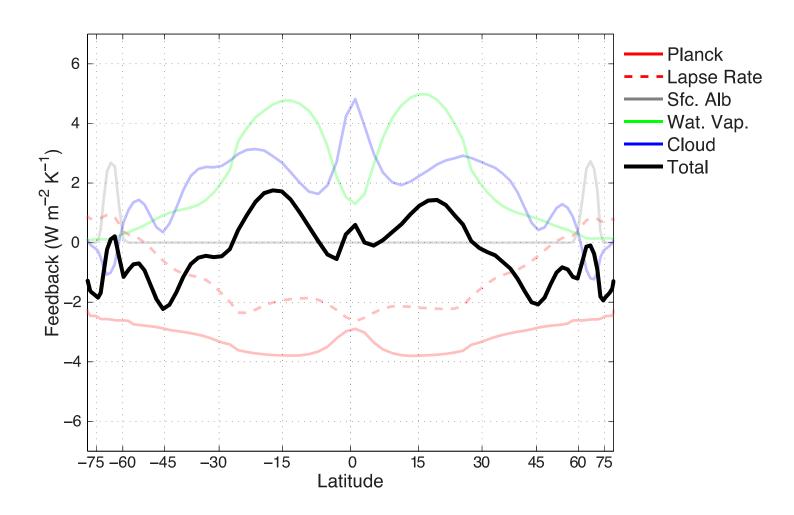
- NonPlanck feedbacks do a lot amplification in tropics & at ice line
- Too much warming in the tropics, not enough at high latitudes

Partial temperature decomposition



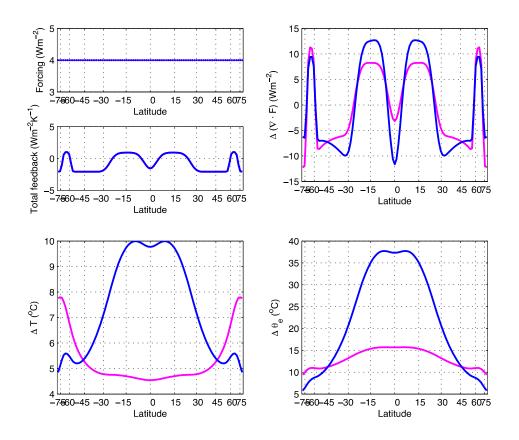
- Transport (i.e., nonlocal impact of feedbacks) can >50% of response
- Two scales to polar amplification 1. >45°: export from tropics
 - 2. >75°: export from ice line

(locally defined)



 Overall, the spatial patterns of feedbacks are slave to the circulation/climate regimes (ITCZ, subtropics, mid-latitudes, ice line)

Moist vs. dry static energy diffusion



Pink = m.s.e. diffusion Blue = cpT only diffusion